

Package ‘IBclust’

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Type Package

Title Information Bottleneck Methods for Clustering Mixed-Type Data

Version 1.2.1

Description Implements multiple variants of the Information Bottleneck ('IB') method for clustering datasets containing continuous, categorical (nominal/ordinal) and mixed-type variables.

The package provides deterministic, agglomerative, generalized, and standard 'IB' clustering algorithms that preserve relevant information while forming interpretable clusters. The Deterministic Information Bottleneck is described in Costa et al. (2024) <[doi:10.48550/arXiv.2407.03389](https://doi.org/10.48550/arXiv.2407.03389)>. The standard 'IB' method originates from Tishby et al. (2000) <[doi:10.48550/arXiv.physics/0004057](https://doi.org/10.48550/arXiv.physics/0004057)>, the agglomerative variant from Slonim and Tishby (1999) <<https://papers.nips.cc/paper/1651-agglomerative-information-bottleneck>>, and the generalized 'IB' from Strouse and Schwab (2017) <[doi:10.1162/NECO_a_00961](https://doi.org/10.1162/NECO_a_00961)>.

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Contents

AIBmix	2
DIBmix	6
GIBmix	12
IBmix	17
Index	23

AIBmix	<i>Agglomerative Information Bottleneck Clustering for Mixed-Type Data</i>
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Description

The AIBmix function implements the Agglomerative Information Bottleneck (AIB) algorithm for hierarchical clustering of datasets containing mixed-type variables, including categorical (nominal and ordinal) and continuous variables. This method merges clusters so that information retention is maximised at each step to create meaningful clusters, leveraging bandwidth parameters to handle different categorical data types (nominal and ordinal) effectively (Slonim and Tishby 1999).

Usage

```
AIBmix(X, s = -1, lambda = -1,
       scale = TRUE, contkernel = "gaussian",
       nomkernel = "aitchisonaitken", ordkernel = "liracine",
       cat_first = FALSE)
```

Arguments

X	A data frame containing the data to be clustered. Variables should be of type numeric (for continuous variables), factor (for nominal variables) or ordered (for ordinal variables).
s	A numeric value or vector specifying the bandwidth parameter(s) for continuous variables. The values must be greater than 0. The default value is -1 , which enables the automatic selection of optimal bandwidth(s). Argument is ignored when no variables are continuous.
lambda	A numeric value or vector specifying the bandwidth parameter for categorical variables. The default value is -1 , which enables automatic determination of the optimal bandwidth. For nominal variables and <code>nomkernel = 'aitchisonaitken'</code> , the maximum allowable value of <code>lambda</code> is $(l-1)/l$, where l represents the number of categories, whereas for <code>nomkernel = 'liracine'</code> the maximum allowable value is 1. For ordinal variables, the maximum allowable value of <code>lambda</code> is 1, regardless of what <code>ordkernel</code> is being used. Argument is ignored when all variables are continuous.
scale	A logical value indicating whether the continuous variables should be scaled to have unit variance before clustering. Defaults to TRUE. Argument is ignored when all variables are categorical.

contkernel	Kernel used for continuous variables. Can be one of gaussian (default) or epanechnikov. Argument is ignored when no variables are continuous.
nomkernel	Kernel used for nominal (unordered categorical) variables. Can be one of aitchisonaitken (default) or liracine. Argument is ignored when no variables are nominal.
ordkernel	Kernel used for ordinal (ordered categorical) variables. Can be one of liracine (default) or wangvanryzin. Argument is ignored when no variables are ordinal.
cat_first	A logical value indicating whether bandwidth selection is prioritised for the categorical variables, instead of the continuous. Defaults to FALSE. Set to TRUE if you suspect that the continuous variables are not informative of the cluster structure. Can only be TRUE when all bandwidths are selected automatically (i.e. $s = -1$, $\lambda = -1$).

Details

The AIBmix function produces a hierarchical agglomerative clustering of the data while retaining maximal information about the original variable distributions. The Agglomerative Information Bottleneck algorithm uses an information-theoretic criterion to merge clusters so that information retention is maximised at each step, hence creating meaningful clusters with maximal information about the original distribution. Bandwidth parameters for categorical (nominal, ordinal) and continuous variables are adaptively determined if not provided. This process identifies stable and interpretable cluster assignments by maximizing mutual information while controlling complexity. The method is well-suited for datasets with mixed-type variables and integrates information from all variable types effectively.

The following kernel functions can be used to estimate densities for the clustering procedure. For continuous variables:

- *Gaussian (RBF) kernel (Silverman 1998):*

$$K_c\left(\frac{x-x'}{s}\right) = \frac{1}{\sqrt{2\pi}} \exp\left\{-\frac{(x-x')^2}{2s^2}\right\}, \quad s > 0.$$

- *Epanechnikov kernel (Epanechnikov 1969):*

$$K_c(x-x'; s) = \begin{cases} \frac{3}{4\sqrt{5}} \left(1 - \frac{(x-x')^2}{5s^2}\right), & \text{if } \frac{(x-x')^2}{s^2} < 5, \\ 0, & \text{otherwise} \end{cases}, \quad s > 0.$$

For nominal (unordered categorical variables):

- *Aitchison & Aitken kernel (Aitchison and Aitken 1976):*

$$K_u(x=x'; \lambda) = \begin{cases} 1-\lambda, & \text{if } x=x' \\ \frac{\lambda}{\ell-1}, & \text{otherwise} \end{cases}, \quad 0 \leq \lambda \leq \frac{\ell-1}{\ell}.$$

- *Li & Racine kernel (Ouyang et al. 2006):*

$$K_u(x=x'; \lambda) = \begin{cases} 1, & \text{if } x=x' \\ \lambda, & \text{otherwise} \end{cases}, \quad 0 \leq \lambda \leq 1.$$

For ordinal (ordered categorical) variables:

- *Li & Racine kernel (Li and Racine 2003)*:

$$K_o(x = x'; \nu) = \begin{cases} 1, & \text{if } x = x' \\ \nu^{|x-x'|}, & \text{otherwise} \end{cases}, \quad 0 \leq \nu \leq 1.$$

- *Wang & van Ryzin kernel (Wang and Van Ryzin 1981)*:

$$K_o(x = x'; \nu) = \begin{cases} 1 - \nu, & \text{if } x = x' \\ \frac{1-\nu}{2} \nu^{|x-x'|}, & \text{otherwise} \end{cases}, \quad 0 \leq \nu \leq 1.$$

The bandwidth parameters s , λ , and ν control the smoothness of the density estimate and are automatically determined by the algorithm if not provided by the user using the approach in Costa et al. (2025). ℓ is the number of levels of the categorical variable. For ordinal variables, the lambda parameter of the function is used to define ν .

Value

An object of class "aibclust" representing the final clustering result. The returned object is a list with the following components:

merges	A data frame with 2 columns and n rows, showing which observations are merged at each step.
merge_costs	A numeric vector tracking the cost incurred by each merge $I(T_m; Y) - I(T_{m-1}; Y)$.
partitions	A list containing n sub-lists. Each sub-list includes the cluster partition at each step.
I_T_Y	A numeric vector including the mutual information $I(T_m; Y)$ as the number of clusters m increases.
I_X_Y	A numeric value of the mutual information $I(X; Y)$ between observation indices and location.
info_ret	A numeric vector of length n including the fraction of the original information retained after each merge.
s	A numeric vector of bandwidth parameters used for the continuous variables. A value of -1 is returned if all variables are categorical.
lambda	A numeric vector of bandwidth parameters used for the categorical variables. A value of -1 is returned if all variables are continuous.
call	The matched call.
n	Number of observations.
contcols	Indices of continuous columns in X .
catcols	Indices of categorical columns in X .
kernels	List with names of kernels used for continuous, nominal, and ordinal features.
obs_names	Names of rows in X ; used for plotting the cluster hierarchy using a dendrogram.

Objects of class "aibclust" support the following methods:

- `print.aibclust`: Display a concise description of the cluster hierarchy.
- `summary.aibclust`: Show detailed information including cluster sizes for 2, 3, and 5 clusters, information-theoretic metrics, and hyperparameters.
- `plot.aibclust`: Produce diagnostic plots:
 - `type = "dendrogram"`: dendrogram visualising the hierarchy of partitions obtained.
 - `type = "info"`: information retention curve; the proportion of information preserved $I(T_m; Y)/I(X; Y)$ by the clustering T_m is plotted against the number of clusters m .

Author(s)

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References

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Examples

```
# Example dataset with categorical, ordinal, and continuous variables
set.seed(123)
data_mix <- data.frame(
  cat_var = factor(sample(letters[1:3], 100, replace = TRUE)), # Nominal categorical variable
  ord_var = factor(sample(c("low", "medium", "high"), 100, replace = TRUE),
                    levels = c("low", "medium", "high"),
                    ordered = TRUE), # Ordinal variable
  cont_var1 = rnorm(100), # Continuous variable 1
  cont_var2 = runif(100) # Continuous variable 2
)

# Perform Mixed-Type Hierarchical Clustering with Agglomerative IB
result_mix <- AIBmix(X = data_mix, lambda = -1, s = -1, scale = TRUE)
```

```

# Print clustering results
plot(result_mix, type = "dendrogram", xlab = "", sub = "", cex = 0.5) # Plot dendrogram
plot(result_mix, type = "info", col = "black", pch = 16) # Plot dendrogram

# Simulated categorical data example
set.seed(123)
data_cat <- data.frame(
  Var1 = as.factor(sample(letters[1:3], 200, replace = TRUE)), # Nominal variable
  Var2 = as.factor(sample(letters[4:6], 200, replace = TRUE)), # Nominal variable
  Var3 = factor(sample(c("low", "medium", "high"), 200, replace = TRUE),
    levels = c("low", "medium", "high"), ordered = TRUE) # Ordinal variable
)

# Run AIBmix with automatic lambda selection
result_cat <- AIBmix(X = data_cat, lambda = -1)

# Print clustering results
plot(result_cat, type = "dendrogram", xlab = "", sub = "", cex = 0.5) # Plot dendrogram

# Results summary
summary(result_cat)

# Simulated continuous data example
set.seed(123)
# Continuous data with 200 observations, 5 features
data_cont <- as.data.frame(matrix(rnorm(1000), ncol = 5))

# Run AIBmix with automatic bandwidth selection
result_cont <- AIBmix(X = data_cont, s = -1, scale = TRUE)

# Print concise summary of output
print(result_cont)

# Print clustering results
plot(result_cont, type = "dendrogram", xlab = "", sub = "", cex = 0.5) # Plot dendrogram

```

DIBmix

Deterministic Information Bottleneck Clustering for Mixed-Type Data

Description

The DIBmix function implements the Deterministic Information Bottleneck (DIB) algorithm for clustering datasets containing continuous, categorical (nominal and ordinal), and mixed-type variables. This method optimizes an information-theoretic objective to preserve relevant information in the cluster assignments while achieving effective data compression (Costa et al. 2025).

Usage

```

DIBmix(X, ncl, randinit = NULL,
  s = -1, lambda = -1, scale = TRUE,

```

```

maxiter = 100, nstart = 100,
contkernel = "gaussian",
nomkernel = "aitchisonaitken", ordkernel = "liracine",
cat_first = FALSE, verbose = FALSE)

```

Arguments

<code>X</code>	A data frame containing the input data to be clustered. It should include categorical variables (factor for nominal and ordered for ordinal) and continuous variables (numeric).
<code>nc1</code>	An integer specifying the number of clusters.
<code>randinit</code>	An optional vector specifying the initial cluster assignments. If NULL, cluster assignments are initialized randomly.
<code>s</code>	A numeric value or vector specifying the bandwidth parameter(s) for continuous variables. The values must be greater than 0. The default value is -1 , which enables the automatic selection of optimal bandwidth(s). Argument is ignored when no variables are continuous.
<code>lambda</code>	A numeric value or vector specifying the bandwidth parameter for categorical variables. The default value is -1 , which enables automatic determination of the optimal bandwidth. For nominal variables and <code>nomkernel = 'aitchisonaitken'</code> , the maximum allowable value of <code>lambda</code> is $(l-1)/l$, where l represents the number of categories, whereas for <code>nomkernel = 'liracine'</code> the maximum allowable value is 1. For ordinal variables, the maximum allowable value of <code>lambda</code> is 1, regardless of what <code>ordkernel</code> is being used. Argument is ignored when all variables are continuous.
<code>scale</code>	A logical value indicating whether the continuous variables should be scaled to have unit variance before clustering. Defaults to TRUE. Argument is ignored when all variables are categorical.
<code>maxiter</code>	The maximum number of iterations allowed for the clustering algorithm. Defaults to 100.
<code>nstart</code>	The number of random initializations to run. The best clustering solution is returned. Defaults to 100.
<code>contkernel</code>	Kernel used for continuous variables. Can be one of <code>gaussian</code> (default) or <code>epanechnikov</code> . Argument is ignored when no variables are continuous.
<code>nomkernel</code>	Kernel used for nominal (unordered categorical) variables. Can be one of <code>aitchisonaitken</code> (default) or <code>liracine</code> . Argument is ignored when no variables are nominal.
<code>ordkernel</code>	Kernel used for ordinal (ordered categorical) variables. Can be one of <code>liracine</code> (default) or <code>wangvanryzin</code> . Argument is ignored when no variables are ordinal.
<code>cat_first</code>	A logical value indicating whether bandwidth selection is prioritised for the categorical variables, instead of the continuous. Defaults to FALSE. Set to TRUE if you suspect that the continuous variables are not informative of the cluster structure. Can only be TRUE when data is of mixed-type and all bandwidths are selected automatically (i.e. <code>s = -1</code> , <code>lambda = -1</code>).
<code>verbose</code>	Logical. Defaults to FALSE to suppress progress messages. Change to TRUE to print.

Details

The DIBmix function clusters data while retaining maximal information about the original variable distributions. The Deterministic Information Bottleneck algorithm optimizes an information-theoretic objective that balances information preservation and compression. Bandwidth parameters for categorical (nominal, ordinal) and continuous variables are adaptively determined if not provided. This iterative process identifies stable and interpretable cluster assignments by maximizing mutual information while controlling complexity. The method is well-suited for datasets with mixed-type variables and integrates information from all variable types effectively.

The following kernel functions can be used to estimate densities for the clustering procedure. For continuous variables:

- *Gaussian (RBF) kernel (Silverman 1998):*

$$K_c\left(\frac{x - x'}{s}\right) = \frac{1}{\sqrt{2\pi}} \exp\left\{-\frac{(x - x')^2}{2s^2}\right\}, \quad s > 0.$$

- *Epanechnikov kernel (Epanechnikov 1969):*

$$K_c(x - x'; s) = \begin{cases} \frac{3}{4\sqrt{5}} \left(1 - \frac{(x-x')^2}{5s^2}\right), & \text{if } \frac{(x-x')^2}{s^2} < 5, \\ 0, & \text{otherwise} \end{cases}, \quad s > 0.$$

For nominal (unordered categorical variables):

- *Aitchison & Aitken kernel (Aitchison and Aitken 1976):*

$$K_u(x = x'; \lambda) = \begin{cases} 1 - \lambda, & \text{if } x = x' \\ \frac{\lambda}{\ell - 1}, & \text{otherwise} \end{cases}, \quad 0 \leq \lambda \leq \frac{\ell - 1}{\ell}.$$

- *Li & Racine kernel (Ouyang et al. 2006):*

$$K_u(x = x'; \lambda) = \begin{cases} 1, & \text{if } x = x' \\ \lambda, & \text{otherwise} \end{cases}, \quad 0 \leq \lambda \leq 1.$$

For ordinal (ordered categorical) variables:

- *Li & Racine kernel (Li and Racine 2003):*

$$K_o(x = x'; \nu) = \begin{cases} 1, & \text{if } x = x' \\ \nu^{|x-x'|}, & \text{otherwise} \end{cases}, \quad 0 \leq \nu \leq 1.$$

- *Wang & van Ryzin kernel (Wang and Van Ryzin 1981):*

$$K_o(x = x'; \nu) = \begin{cases} 1 - \nu, & \text{if } x = x' \\ \frac{1-\nu}{2} \nu^{|x-x'|}, & \text{otherwise} \end{cases}, \quad 0 \leq \nu \leq 1.$$

The bandwidth parameters s , λ , and ν control the smoothness of the density estimate and are automatically determined by the algorithm if not provided by the user using the approach in Costa et al. (2025). ℓ is the number of levels of the categorical variable. For ordinal variables, the lambda parameter of the function is used to define ν .

Value

An object of class "gibclust" representing the final clustering result. The returned object is a list with the following components:

Cluster	An integer vector giving the cluster assignments for each data point.
Entropy	A numeric value representing the entropy of the cluster assignments at convergence.
CondEntropy	A numeric value representing the conditional entropy of cluster assignment, given the observation weights $H(T X)$.
MutualInfo	A numeric value representing the mutual information, $I(Y; T)$, between the original labels (Y) and the cluster assignments (T).
InfoXT	A numeric value representing the mutual information, $I(X; T)$, between the original observations weights (X) and the cluster assignments (T).
beta	A numeric vector of the final beta values used in the iterative procedure.
alpha	A numeric value of the strength of conditional entropy used, controlling fuzziness of the solution. This is by default equal to 0 for DIBmix.
s	A numeric vector of bandwidth parameters used for the continuous variables. A value of -1 is returned if all variables are categorical.
lambda	A numeric vector of bandwidth parameters used for the categorical variables. A value of -1 is returned if all variables are continuous.
call	The matched call.
ncl	Number of clusters.
n	Number of observations.
iters	Number of iterations used to obtain the returned solution.
converged	Logical indicating whether convergence was reached before <code>maxiter</code> .
conv_tol	Numeric convergence tolerance; by default 0 for DIBmix.
contcols	Indices of continuous columns in X .
catcols	Indices of categorical columns in X .
kernels	List with names of kernels used for continuous, nominal, and ordinal features.

Objects of class "gibclust" support the following methods:

- `print.gibclust`: Display a concise description of the cluster assignment.
- `summary.gibclust`: Show detailed information including cluster sizes, information-theoretic metrics, hyperparameters, and convergence details.
- `plot.gibclust`: Produce diagnostic plots:
 - `type = "sizes"`: barplot of cluster sizes or hardened sizes (IB/GIB).
 - `type = "info"`: barplot of entropy, conditional entropy, and mutual information.
 - `type = "beta"`: trajectory of $\log \beta$ over iterations (only available for hard clustering outputs obtained using DIBmix).

Author(s)

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References

- Costa E, Papatsouma I, Markos A (2025). “A Deterministic Information Bottleneck Method for Clustering Mixed-Type Data.” doi:10.48550/arXiv.2407.03389, arXiv:2407.03389, <https://arxiv.org/abs/2407.03389>.
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- Li Q, Racine J (2003). “Nonparametric estimation of distributions with categorical and continuous data.” *Journal of Multivariate Analysis*, **86**(2), 266–292.
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- Epanechnikov VA (1969). “Non-parametric estimation of a multivariate probability density.” *Theory of Probability & Its Applications*, **14**(1), 153–158.

Examples

```
# Example 1: Basic Mixed-Type Clustering
set.seed(123)

# Create a more realistic dataset with mixed variable types
data_mix <- data.frame(
  # Categorical variables
  education = factor(sample(c("High School", "Bachelor", "Master", "PhD"), 150,
    replace = TRUE, prob = c(0.4, 0.3, 0.2, 0.1))),
  employment = factor(sample(c("Full-time", "Part-time", "Unemployed"), 150,
    replace = TRUE, prob = c(0.6, 0.25, 0.15))),

  # Ordinal variable
  satisfaction = factor(sample(c("Low", "Medium", "High"), 150, replace = TRUE),
    levels = c("Low", "Medium", "High"), ordered = TRUE),

  # Continuous variables
  income = rlnorm(150, meanlog = 10, sdlog = 0.5), # Log-normal income
  age = rnorm(150, mean = 35, sd = 10), # Normally distributed age
  experience = rpois(150, lambda = 8) # Years of experience
)

# Perform Mixed-Type Clustering
result_mix <- DIBmix(X = data_mix, ncl = 3, nstart = 5)

# View results
print(paste("Number of clusters found:", length(unique(result_mix$Cluster))))
print(paste("Mutual Information:", round(result_mix$MutualInfo, 3)))
table(result_mix$Cluster)

# Example 2: Comparing cat_first parameter
# When categorical variables are more informative
```

```

result_cat_first <- DIBmix(X = data_mix, ncl = 3,
                          cat_first = TRUE, # Prioritize categorical variables
                          nstart = 5)

# When continuous variables are more informative (default)
result_cont_first <- DIBmix(X = data_mix, ncl = 3,
                           cat_first = FALSE,
                           nstart = 5)

# Compare clustering performance
if (requireNamespace("mclust", quietly = TRUE)){ # For adjustedRandIndex
  print(paste("Agreement between approaches:",
             round(mclust::adjustedRandIndex(result_cat_first$Cluster,
                                             result_cont_first$Cluster), 3)))
}

plot(result_cat_first, type = "sizes") # Bar plot of cluster sizes
plot(result_cat_first, type = "info") # Information-theoretic quantities plot
plot(result_cat_first, type = "beta") # Plot of evolution of beta

# Simulated categorical data example
data_cat <- data.frame(
  Var1 = as.factor(sample(letters[1:3], 200, replace = TRUE)), # Nominal variable
  Var2 = as.factor(sample(letters[4:6], 200, replace = TRUE)), # Nominal variable
  Var3 = factor(sample(c("low", "medium", "high"), 200, replace = TRUE),
                levels = c("low", "medium", "high"), ordered = TRUE) # Ordinal variable
)

# Perform hard clustering on categorical data with Deterministic IB
result_cat <- DIBmix(X = data_cat, ncl = 3, lambda = -1, nstart = 5)

# Print clustering results
print(result_cat$Cluster)      # Cluster assignments
print(result_cat$Entropy)     # Final entropy
print(result_cat$MutualInfo)  # Mutual information

# Simulated continuous data example
set.seed(123)
# Continuous data with 200 observations, 5 features
data_cont <- as.data.frame(matrix(rnorm(1000), ncol = 5))

# Perform hard clustering on continuous data with Deterministic IB
result_cont <- DIBmix(X = data_cont, ncl = 3, s = -1, nstart = 5)

# Print clustering results
print(result_cont$Cluster)    # Cluster assignments
print(result_cont$Entropy)   # Final entropy
print(result_cont$MutualInfo) # Mutual information

# Summary of output
print(result_cont)
summary(result_cont)

```

Description

The GIBmix function implements the Generalised Information Bottleneck (GIB) algorithm for clustering datasets containing continuous, categorical (nominal and ordinal), and mixed-type variables. This method optimizes an information-theoretic objective to preserve relevant information in the cluster assignments while achieving effective data compression (Strouse and Schwab 2017).

Usage

```
GIBmix(X, ncl, beta, alpha, randinit = NULL,
       s = -1, lambda = -1, scale = TRUE,
       maxiter = 100, nstart = 100,
       conv_tol = 1e-5, contkernel = "gaussian",
       nomkernel = "aitchisonaitken", ordkernel = "liracine",
       cat_first = FALSE, verbose = FALSE)
```

Arguments

X	A data frame containing the input data to be clustered. It should include categorical variables (factor for nominal and ordered for ordinal) and continuous variables (numeric).
ncl	An integer specifying the number of clusters.
beta	Regularisation strength characterizing the tradeoff between compression and relevance. Must be non-negative.
alpha	Strength of conditional entropy term. Must be in the range $[0, 1]$. Setting $\alpha = 0$ calls the DIBmix function and ignores the value of beta, while $\alpha = 1$ calls IBmix instead.
randinit	An optional vector specifying the initial cluster assignments. If NULL, cluster assignments are initialized randomly.
s	A numeric value or vector specifying the bandwidth parameter(s) for continuous variables. The values must be greater than 0. The default value is -1 , which enables the automatic selection of optimal bandwidth(s). Argument is ignored when no variables are continuous.
lambda	A numeric value or vector specifying the bandwidth parameter for categorical variables. The default value is -1 , which enables automatic determination of the optimal bandwidth. For nominal variables and <code>nomkernel = 'aitchisonaitken'</code> , the maximum allowable value of lambda is $(l-1)/l$, where l represents the number of categories, whereas for <code>nomkernel = 'liracine'</code> the maximum allowable value is 1. For ordinal variables, the maximum allowable value of lambda is 1, regardless of what <code>ordkernel</code> is being used. Argument is ignored when all variables are continuous.

scale	A logical value indicating whether the continuous variables should be scaled to have unit variance before clustering. Defaults to TRUE. Argument is ignored when all variables are categorical.
maxiter	The maximum number of iterations allowed for the clustering algorithm. Defaults to 100.
nstart	The number of random initializations to run. The best clustering solution is returned. Defaults to 100.
conv_tol	Convergence tolerance level; for a cluster membership matrix $U^{(m)}$ at iteration m , convergence is achieved if $\sum_{i,j} U_{i,j}^{m+1} - U_{i,j}^m \leq \text{conv_tol}$. Must be in range $[0, 1]$. Defaults to $1e-5$.
contkernel	Kernel used for continuous variables. Can be one of gaussian (default) or epanechnikov. Argument is ignored when no variables are continuous.
nomkernel	Kernel used for nominal (unordered categorical) variables. Can be one of aitchisonaitken (default) or liracine. Argument is ignored when no variables are nominal.
ordkernel	Kernel used for ordinal (ordered categorical) variables. Can be one of liracine (default) or wangvanryzin. Argument is ignored when no variables are ordinal.
cat_first	A logical value indicating whether bandwidth selection is prioritised for the categorical variables, instead of the continuous. Defaults to FALSE. Set to TRUE if you suspect that the continuous variables are not informative of the cluster structure. Can only be TRUE when data is of mixed-type and all bandwidths are selected automatically (i.e. $s = -1$, $\lambda = -1$).
verbose	Logical. Defaults to FALSE to suppress progress messages. Change to TRUE to print.

Details

The GIBmix function produces a fuzzy clustering of the data while retaining maximal information about the original variable distributions. The Generalised Information Bottleneck algorithm optimizes an information-theoretic objective that balances information preservation and compression. Bandwidth parameters for categorical (nominal, ordinal) and continuous variables are adaptively determined if not provided. This iterative process identifies stable and interpretable cluster assignments by maximizing mutual information while controlling complexity. The method is well-suited for datasets with mixed-type variables and integrates information from all variable types effectively. Set $\alpha = 1$ and $\alpha = 0$ to recover the Information Bottleneck and its Deterministic variant, respectively. If $\alpha = 0$, the algorithm ignores the value of the regularisation parameter β .

The following kernel functions can be used to estimate densities for the clustering procedure. For continuous variables:

- *Gaussian (RBF) kernel (Silverman 1998):*

$$K_c\left(\frac{x - x'}{s}\right) = \frac{1}{\sqrt{2\pi}} \exp\left\{-\frac{(x - x')^2}{2s^2}\right\}, \quad s > 0.$$

- *Epanechnikov kernel (Epanechnikov 1969):*

$$K_c(x - x'; s) = \begin{cases} \frac{3}{4\sqrt{5}} \left(1 - \frac{(x-x')^2}{5s^2}\right), & \text{if } \frac{(x-x')^2}{s^2} < 5 \\ 0, & \text{otherwise} \end{cases}, \quad s > 0.$$

For nominal (unordered categorical variables):

- *Aitchison & Aitken kernel (Aitchison and Aitken 1976):*

$$K_u(x = x'; \lambda) = \begin{cases} 1 - \lambda, & \text{if } x = x' \\ \frac{\lambda}{\ell - 1}, & \text{otherwise} \end{cases}, \quad 0 \leq \lambda \leq \frac{\ell - 1}{\ell}.$$

- *Li & Racine kernel (Ouyang et al. 2006):*

$$K_u(x = x'; \lambda) = \begin{cases} 1, & \text{if } x = x' \\ \lambda, & \text{otherwise} \end{cases}, \quad 0 \leq \lambda \leq 1.$$

For ordinal (ordered categorical) variables:

- *Li & Racine kernel (Li and Racine 2003):*

$$K_o(x = x'; \nu) = \begin{cases} 1, & \text{if } x = x' \\ \nu^{|x - x'|}, & \text{otherwise} \end{cases}, \quad 0 \leq \nu \leq 1.$$

- *Wang & van Ryzin kernel (Wang and Van Ryzin 1981):*

$$K_o(x = x'; \nu) = \begin{cases} 1 - \nu, & \text{if } x = x' \\ \frac{1 - \nu}{2} \nu^{|x - x'|}, & \text{otherwise} \end{cases}, \quad 0 \leq \nu \leq 1.$$

The bandwidth parameters s , λ , and ν control the smoothness of the density estimate and are automatically determined by the algorithm if not provided by the user using the approach in Costa et al. (2025). ℓ is the number of levels of the categorical variable. For ordinal variables, the lambda parameter of the function is used to define ν .

Value

An object of class "gibclust" representing the final clustering result. The returned object is a list with the following components:

Cluster	An integer vector giving the cluster assignments for each data point.
Entropy	A numeric value representing the entropy of the cluster assignments at convergence.
CondEntropy	A numeric value representing the conditional entropy of cluster assignment, given the observation weights $H(T X)$.
MutualInfo	A numeric value representing the mutual information, $I(Y; T)$, between the original labels (Y) and the cluster assignments (T).
InfoXT	A numeric value representing the mutual information, $I(X; T)$, between the original observations weights (X) and the cluster assignments (T).
beta	A numeric vector of the final beta values used in the iterative procedure.
alpha	A numeric value of the strength of conditional entropy used, controlling fuzziness of the solution. This is by default equal to 0 for DIBmix.

<code>s</code>	A numeric vector of bandwidth parameters used for the continuous variables. A value of -1 is returned if all variables are categorical.
<code>lambda</code>	A numeric vector of bandwidth parameters used for the categorical variables. A value of -1 is returned if all variables are continuous.
<code>call</code>	The matched call.
<code>nc1</code>	Number of clusters.
<code>n</code>	Number of observations.
<code>iters</code>	Number of iterations used to obtain the returned solution.
<code>converged</code>	Logical indicating whether convergence was reached before <code>maxiter</code> .
<code>conv_tol</code>	Numeric convergence tolerance.
<code>contcols</code>	Indices of continuous columns in X .
<code>catcols</code>	Indices of categorical columns in X .
<code>kernels</code>	List with names of kernels used for continuous, nominal, and ordinal features.

Objects of class "gibclust" support the following methods:

- `print.gibclust`: Display a concise description of the cluster assignment.
- `summary.gibclust`: Show detailed information including cluster sizes, information-theoretic metrics, hyperparameters, and convergence details.
- `plot.gibclust`: Produce diagnostic plots:
 - `type = "sizes"`: barplot of cluster sizes or hardened sizes (IB/GIB).
 - `type = "info"`: barplot of entropy, conditional entropy, and mutual information.
 - `type = "beta"`: trajectory of $\log \beta$ over iterations (only available for hard clustering outputs obtained using DIBmix).

Author(s)

Efthymios Costa, Ioanna Papatsouma, Angelos Markos

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- Epanechnikov VA (1969). "Non-parametric estimation of a multivariate probability density." *Theory of Probability & Its Applications*, **14**(1), 153–158.

Examples

```

# Example dataset with categorical, ordinal, and continuous variables
set.seed(123)
data_mix <- data.frame(
  cat_var = factor(sample(letters[1:3], 100, replace = TRUE)), # Nominal categorical variable
  ord_var = factor(sample(c("low", "medium", "high"), 100, replace = TRUE),
                    levels = c("low", "medium", "high"),
                    ordered = TRUE), # Ordinal variable
  cont_var1 = rnorm(100), # Continuous variable 1
  cont_var2 = runif(100) # Continuous variable 2
)

# Perform Mixed-Type Fuzzy Clustering with Generalised IB
result_mix <- GIBmix(X = data_mix, ncl = 3, beta = 2, alpha = 0.5, nstart = 5)

# Print clustering results
print(result_mix$Cluster) # Cluster membership matrix
print(result_mix$Entropy) # Entropy of final clustering
print(result_mix$CondEntropy) # Conditional entropy of final clustering
print(result_mix$MutualInfo) # Mutual information between Y and T

# Summary of output
summary(result_mix)

# Simulated categorical data example
set.seed(123)
data_cat <- data.frame(
  Var1 = as.factor(sample(letters[1:3], 200, replace = TRUE)), # Nominal variable
  Var2 = as.factor(sample(letters[4:6], 200, replace = TRUE)), # Nominal variable
  Var3 = factor(sample(c("low", "medium", "high"), 200, replace = TRUE),
                levels = c("low", "medium", "high"), ordered = TRUE) # Ordinal variable
)

# Perform Fuzzy Clustering on categorical data with Generalised IB
result_cat <- GIBmix(X = data_cat, ncl = 2, beta = 25, alpha = 0.75, lambda = -1, nstart = 5)

# Print clustering results
print(result_cat$Cluster) # Cluster membership matrix
print(result_cat$Entropy) # Entropy of final clustering
print(result_cat$CondEntropy) # Conditional entropy of final clustering
print(result_cat$MutualInfo) # Mutual information between Y and T

# Simulated continuous data example
set.seed(123)
# Continuous data with 200 observations, 5 features
data_cont <- as.data.frame(matrix(rnorm(1000), ncol = 5))

# Perform Fuzzy Clustering on continuous data with Generalised IB
result_cont <- GIBmix(X = data_cont, ncl = 2, beta = 50, alpha = 0.75, s = -1, nstart = 5)

# Print clustering results
print(result_cont$Cluster) # Cluster membership matrix

```



```

print(result_cont$Entropy)      # Entropy of final clustering
print(result_cont$CondEntropy)  # Conditional entropy of final clustering
print(result_cont$MutualInfo)   # Mutual information between Y and T

plot(result_cont, type = "sizes") # Bar plot of cluster sizes (hardened assignments)
plot(result_cont, type = "info") # Information-theoretic quantities plot

```

 IBmix

Information Bottleneck Clustering for Mixed-Type Data

Description

The `IBmix` function implements the Information Bottleneck (IB) algorithm for clustering datasets containing continuous, categorical (nominal and ordinal), and mixed-type variables. This method optimizes an information-theoretic objective to preserve relevant information in the cluster assignments while achieving effective data compression (Strouse and Schwab 2019).

Usage

```

IBmix(X, ncl, beta, randinit = NULL,
      s = -1, lambda = -1, scale = TRUE,
      maxiter = 100, nstart = 100,
      conv_tol = 1e-5, contkernel = "gaussian",
      nomkernel = "aitchisonaitken", ordkernel = "liracine",
      cat_first = FALSE, verbose = FALSE)

```

Arguments

<code>X</code>	A data frame containing the input data to be clustered. It should include categorical variables (factor for nominal and <code>Ord</code> factor for ordinal) and continuous variables (numeric).
<code>ncl</code>	An integer specifying the number of clusters.
<code>beta</code>	Regularisation strength characterizing the tradeoff between compression and relevance. Must be non-negative.
<code>randinit</code>	An optional vector specifying the initial cluster assignments. If <code>NULL</code> , cluster assignments are initialized randomly.
<code>s</code>	A numeric value or vector specifying the bandwidth parameter(s) for continuous variables. The values must be greater than 0. The default value is <code>-1</code> , which enables the automatic selection of optimal bandwidth(s). Argument is ignored when no variables are continuous.
<code>lambda</code>	A numeric value or vector specifying the bandwidth parameter for categorical variables. The default value is <code>-1</code> , which enables automatic determination of the optimal bandwidth. For nominal variables and <code>nomkernel = 'aitchisonaitken'</code> , the maximum allowable value of <code>lambda</code> is $(l-1)/l$, where l represents the number of categories, whereas for <code>nomkernel = 'liracine'</code> the maximum allowable value is 1. For ordinal variables, the maximum allowable value of <code>lambda</code> is 1, regardless of what <code>ordkernel</code> is being used. Argument is ignored when all variables are continuous.

scale	A logical value indicating whether the continuous variables should be scaled to have unit variance before clustering. Defaults to TRUE. Argument is ignored when all variables are categorical.
maxiter	The maximum number of iterations allowed for the clustering algorithm. Defaults to 100.
nstart	The number of random initializations to run. The best clustering solution is returned. Defaults to 100.
conv_tol	Convergence tolerance level; for a cluster membership matrix $U^{(m)}$ at iteration m , convergence is achieved if $\sum_{i,j} U_{i,j}^{m+1} - U_{i,j}^m \leq \text{conv_tol}$. Must be in range $[0, 1]$. Defaults to $1e-5$.
contkernel	Kernel used for continuous variables. Can be one of gaussian (default) or epanechnikov. Argument is ignored when no variables are continuous.
nomkernel	Kernel used for nominal (unordered categorical) variables. Can be one of aitchisonaitken (default) or liracine. Argument is ignored when no variables are nominal.
ordkernel	Kernel used for ordinal (ordered categorical) variables. Can be one of liracine (default) or wangvanryzin. Argument is ignored when no variables are ordinal.
cat_first	A logical value indicating whether bandwidth selection is prioritised for the categorical variables, instead of the continuous. Defaults to FALSE. Set to TRUE if you suspect that the continuous variables are not informative of the cluster structure. Can only be TRUE when data is of mixed-type and all bandwidths are selected automatically (i.e. $s = -1$, $\lambda = -1$).
verbose	Logical. Defaults to FALSE to suppress progress messages. Change to TRUE to print.

Details

The IBmix function produces a fuzzy clustering of the data while retaining maximal information about the original variable distributions. The Information Bottleneck algorithm optimizes an information-theoretic objective that balances information preservation and compression. Bandwidth parameters for categorical (nominal, ordinal) and continuous variables are adaptively determined if not provided. This iterative process identifies stable and interpretable cluster assignments by maximizing mutual information while controlling complexity. The method is well-suited for datasets with mixed-type variables and integrates information from all variable types effectively.

The following kernel functions can be used to estimate densities for the clustering procedure. For continuous variables:

- *Gaussian (RBF) kernel (Silverman 1998):*

$$K_c\left(\frac{x - x'}{s}\right) = \frac{1}{\sqrt{2\pi}} \exp\left\{-\frac{(x - x')^2}{2s^2}\right\}, \quad s > 0.$$

- *Epanechnikov kernel (Epanechnikov 1969):*

$$K_c(x - x'; s) = \begin{cases} \frac{3}{4\sqrt{5}} \left(1 - \frac{(x-x')^2}{5s^2}\right), & \text{if } \frac{(x-x')^2}{s^2} < 5 \\ 0, & \text{otherwise} \end{cases}, \quad s > 0.$$

For nominal (unordered categorical variables):

- *Aitchison & Aitken kernel (Aitchison and Aitken 1976):*

$$K_u(x = x'; \lambda) = \begin{cases} 1 - \lambda, & \text{if } x = x' \\ \frac{\lambda}{\ell - 1}, & \text{otherwise} \end{cases}, \quad 0 \leq \lambda \leq \frac{\ell - 1}{\ell}.$$

- *Li & Racine kernel (Ouyang et al. 2006):*

$$K_u(x = x'; \lambda) = \begin{cases} 1, & \text{if } x = x' \\ \lambda, & \text{otherwise} \end{cases}, \quad 0 \leq \lambda \leq 1.$$

For ordinal (ordered categorical) variables:

- *Li & Racine kernel (Li and Racine 2003):*

$$K_o(x = x'; \nu) = \begin{cases} 1, & \text{if } x = x' \\ \nu^{|x-x'|}, & \text{otherwise} \end{cases}, \quad 0 \leq \nu \leq 1.$$

- *Wang & van Ryzin kernel (Wang and Van Ryzin 1981):*

$$K_o(x = x'; \nu) = \begin{cases} 1 - \nu, & \text{if } x = x' \\ \frac{1-\nu}{2} \nu^{|x-x'|}, & \text{otherwise} \end{cases}, \quad 0 \leq \nu \leq 1.$$

The bandwidth parameters s , λ , and ν control the smoothness of the density estimate and are automatically determined by the algorithm if not provided by the user using the approach in Costa et al. (2025). ℓ is the number of levels of the categorical variable. For ordinal variables, the lambda parameter of the function is used to define ν .

Value

An object of class "gibclust" representing the final clustering result. The returned object is a list with the following components:

Cluster	An integer vector giving the cluster assignments for each data point.
Entropy	A numeric value representing the entropy of the cluster assignments at convergence.
CondEntropy	A numeric value representing the conditional entropy of cluster assignment, given the observation weights $H(T X)$.
MutualInfo	A numeric value representing the mutual information, $I(Y; T)$, between the original labels (Y) and the cluster assignments (T).
InfoXT	A numeric value representing the mutual information, $I(X; T)$, between the original observations weights (X) and the cluster assignments (T).
beta	A numeric vector of the final beta values used in the iterative procedure.
alpha	A numeric value of the strength of conditional entropy used, controlling fuzziness of the solution. This is by default equal to 0 for DIBmix.

<code>s</code>	A numeric vector of bandwidth parameters used for the continuous variables. A value of -1 is returned if all variables are categorical.
<code>lambda</code>	A numeric vector of bandwidth parameters used for the categorical variables. A value of -1 is returned if all variables are continuous.
<code>call</code>	The matched call.
<code>nc1</code>	Number of clusters.
<code>n</code>	Number of observations.
<code>iters</code>	Number of iterations used to obtain the returned solution.
<code>converged</code>	Logical indicating whether convergence was reached before <code>maxiter</code> .
<code>conv_tol</code>	Numeric convergence tolerance.
<code>contcols</code>	Indices of continuous columns in X .
<code>catcols</code>	Indices of categorical columns in X .
<code>kernels</code>	List with names of kernels used for continuous, nominal, and ordinal features.

Objects of class "gibclust" support the following methods:

- `print.gibclust`: Display a concise description of the cluster assignment.
- `summary.gibclust`: Show detailed information including cluster sizes, information-theoretic metrics, hyperparameters, and convergence details.
- `plot.gibclust`: Produce diagnostic plots:
 - `type = "sizes"`: barplot of cluster sizes or hardened sizes (IB/GIB).
 - `type = "info"`: barplot of entropy, conditional entropy, and mutual information.
 - `type = "beta"`: trajectory of $\log \beta$ over iterations (only available for hard clustering outputs obtained using DIBmix).

Author(s)

Efthymios Costa, Ioanna Papatsouma, Angelos Markos

References

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- Ouyang D, Li Q, Racine J (2006). "Cross-validation and the estimation of probability distributions with categorical data." *Journal of Nonparametric Statistics*, **18**(1), 69–100.
- Wang M, Van Ryzin J (1981). "A class of smooth estimators for discrete distributions." *Biometrika*, **68**(1), 301–309.
- Epanechnikov VA (1969). "Non-parametric estimation of a multivariate probability density." *Theory of Probability & Its Applications*, **14**(1), 153–158.

Examples

```

# Example dataset with categorical, ordinal, and continuous variables
set.seed(123)
data_mix <- data.frame(
  cat_var = factor(sample(letters[1:3], 100, replace = TRUE)), # Nominal categorical variable
  ord_var = factor(sample(c("low", "medium", "high"), 100, replace = TRUE),
    levels = c("low", "medium", "high"),
    ordered = TRUE), # Ordinal variable
  cont_var1 = rnorm(100), # Continuous variable 1
  cont_var2 = runif(100) # Continuous variable 2
)

# Perform Mixed-Type Fuzzy Clustering
result_mix <- IBmix(X = data_mix, ncl = 3, beta = 2, nstart = 1)

# Print clustering results
print(result_mix$Cluster) # Cluster membership matrix
print(result_mix$InfoXT) # Mutual information between X and T
print(result_mix$MutualInfo) # Mutual information between Y and T

# Summary of output
summary(result_mix)

# Simulated categorical data example
set.seed(123)
data_cat <- data.frame(
  Var1 = as.factor(sample(letters[1:3], 100, replace = TRUE)), # Nominal variable
  Var2 = as.factor(sample(letters[4:6], 100, replace = TRUE)), # Nominal variable
  Var3 = factor(sample(c("low", "medium", "high"), 100, replace = TRUE),
    levels = c("low", "medium", "high"), ordered = TRUE) # Ordinal variable
)

# Perform fuzzy clustering on categorical data with standard IB
result_cat <- IBmix(X = data_cat, ncl = 3, beta = 15, lambda = -1, nstart = 2, maxiter = 200)

# Print clustering results
print(result_cat$Cluster) # Cluster membership matrix
print(result_cat$InfoXT) # Mutual information between X and T
print(result_cat$MutualInfo) # Mutual information between Y and T

plot(result_cat, type = "sizes") # Bar plot of cluster sizes (hardened assignments)
plot(result_cat, type = "info") # Information-theoretic quantities plot

# Simulated continuous data example
set.seed(123)
# Continuous data with 100 observations, 5 features
data_cont <- as.data.frame(matrix(rnorm(500), ncol = 5))

# Perform fuzzy clustering on continuous data with standard IB
result_cont <- IBmix(X = data_cont, ncl = 3, beta = 50, s = -1, nstart = 2)

# Print clustering results

```

```
print(result_cont$Cluster)      # Cluster membership matrix
print(result_cont$InfoXT)      # Mutual information between X and T
print(result_cont$MutualInfo)  # Mutual information between Y and T
```

Index

* **clustering**

AIBmix, [2](#)

DIBmix, [6](#)

GIBmix, [12](#)

IBmix, [17](#)

AIBmix, [2](#)

DIBmix, [6](#)

GIBmix, [12](#)

IBmix, [17](#)